

6.100A

Final Review



Type of knowledge

Declarative knowledge - a statement of fact

- Stata is building 32

Imperative knowledge - a recipe, 'how-to' knowledge

1. Start at Student Center
2. Walk down Mass Ave, towards Vassar St
3. Make a right on Vassar
4. Walk until you see a funky-looking building

Programming is about writing recipes to generate facts!

Expressions and Statements

Expression - combination of objects and operators, and can be evaluated to a value

- `3 + 5`
- `a or (True and b)`

Statements - instructs the interpreter to perform some action

- `print(3 + 5)`
- `return a or (True and b)`

Primitive Types

- 1) Boolean → True, False
- 2) Strings → "abc", "123", "@#% !\$&@*"
- 3) Numbers:
 - a) ints: 0, 1, 2, 3
 - b) floats: 1., 1.46, 8.76, 1.1111
- 4) None

Type Issues

- a. $1 // 2 = 0$ (integer division)
- b. $1.0 // 2 = 0.0$ (integer division casted (implicitly) to float)
- c. $1 / 2 = 0.5$ (float division)
- d. $\text{int}(1 / 2) = 0$ (casting)

NOTE: integer division truncates the answer – it does NOT round to nearest int (use round for that)

$$7 / 3 = 2.33333333$$

$$7 // 3 = 2$$

$$7 / 4 = 1.75$$

$$7 // 4 = 1$$

Operations

- Arithmetic operations (follow order of operations / PEMDAS rules)
 - +, -, *, /
 - ** for exponents
 - % modulo to get remainder
- String operations
 - + for concatenation
 - * to repeat
- Boolean comparators
 - >, >=, <, <=, ==, !=
- Logical operators
 - and, or, not

Representing Numbers - Binary

Integers are represented in **base 2**, also known as binary:

$$1 \ 0 \ 1 \ 1 \ 0 \ 1 \ 0 \ 1 = 181$$

$$2^7 \ 2^6 \ 2^5 \ 2^4 \ 2^3 \ 2^2 \ 2^1 \ 2^0$$

$$128 + 0 + 32 + 16 + 0 + 4 + 0 + 1$$

Representing Numbers - Floats

Two parts, the **mantissa** and the **exponent**, both represented in **binary**

$$M * 2^p \rightarrow (M, p)$$

mantissa exponent

$$1.25 = 5 * 2^{-2} = (101, -10)$$

T/F Question!

T/F Question: The value of `'math.sqrt(2.0)*math.sqrt(2.0) == 2.0'` is True.

False! `2.000000000000000004 != 2.0`

Approximation - Floats

```
In [1]: import math
```

```
In [2]: math.sqrt(2.0) * math.sqrt(2.0) == 2.0
```

```
Out[2]: False
```

```
In [3]: print(math.sqrt(2.0) * math.sqrt(2.0))  
2.00000000000000004
```

```
In [4]: abs((math.sqrt(2.0) * math.sqrt(2.0)) - 2.0) < 1e-9
```

```
Out[4]: True
```



Questions?



Swap Variables: Question

```
x = 1  
y = 2  
y = x  
x = y
```

Swap Variables

```
x = 1  
y = 2  
y = x  
x = y
```



```
x = 1  
y = 2  
temp = y  
y = x  
x = temp
```



```
x = 1  
y = 2  
y, x = x, y
```

Very pythonic!

Control: IF

if condition 1:

some code to run

if condition 2:

other code to be run

else:

some code to run if **condition 2** was not met

Control: IF

if condition 1:

some code to run

elif condition 2:

some other code to run **instead**

else:

some more conditions to run if the other conditions weren't met

Control: Loops

for

- Repeat this block of code once per element in the given iterable
- *for var in iterable:*
 #code

while

- Repeat this block of code until a given condition is False
- *while condition:*
 #code

Control: For Loops

```
>>> word = 'hello'
>>> for letter in word:
    print(letter)
```

```
>>> word = 'hello'
>>> for i in range(len(word)):
    print(word[i])
```

```
>>> |
```

```
>>> |
```

```
>>> char_list = ['a', 'b', 'c']
>>> for char in char_list:
    print(char)
```

```
>>> char_list = ['a', 'b', 'c']
>>> for i in range(len(char_list)):
    print(char_list[i])
```

```
>>> |
```

```
>>> |
```

Think about if you want the element in the iterable itself, or just its index

Example Question

What is going to be printed?

```
T = (0.1, 0.1)
x = 0.0

for i in range(len(T)):

    for j in T:
        x += i + j
        print (x)

print( i )
```

Example Question

```
T = (0.1, 0.1)
x = 0.0
```

```
for i in range(len(T)):
    for j in T:
        x += i + j
        print (x)

print( i )
```

What is going to be printed?

Behind the scenes (bolded text is what is printed):
Remember, $x += i + j$ is the equivalent of $x = x + i + j$

```
i = 0
    j = 0.1
        x = x + i + j → x = 0.0 + 0 + 0.1 = 0.1
    j = 0.1
        x = x + i + j → x = 0.1 + 0 + 0.1 = 0.2
i = 1
    j = 0.1
        x = x + i + j → x = 0.2 + 1 + 0.1 = 1.3
    j = 0.1
        x = x + i + j → x = 1.3 + 1 + 0.1 = 2.4
```

Last value of i was 1 → **1**

Guess and Check

- Guess a value for the solution
- Check if the solution is correct
- Keep guessing until solution is good enough

Process is exhaustive enumeration, can take really long to find answer

Example of Guess & Check: Finding Square Roots

```
number = int(input("Enter a number: "))
answer = 0
steps = 0
while answer**2 < abs(number):
    answer = answer + 1
    steps+=1
#if square of ans is not equals to actual number, then x is not a perfect square
if answer**2 != abs(number):
    print(str(number) + ' is not a perfect square')
else:
    print('Square root of ' + str(number) + ' is ' + str(answer))
    print('The steps it took to reach the ans are: ' + str(steps))
```



Questions?



Lists

- Ordered sequence of elements
- Initialized with square brackets
- Mutable

```
>>> myList = [3,5,2,7]
>>> myList[0]
3
>>> myList[1] = 6
[3, 6, 2, 7]
>>> myList[:2]
[3, 6]
```

T/F Question :

Given a list `L = ['f', 'b']` the statement `L[1] = 'c'` will mutate list `L`. **True**

T/F Question :

Let `L` be a list, each element of which is a list of ints. In Python, the assignment statement `L[0][0] = 3` mutates the list `L`. **False**

List Functions

```
>>> letters = ['a','b','d']
```

```
>>> len(letters)
```

```
3
```

```
>>> letters.append(['e'])
```

```
['a', 'b', 'd', ['e']]
```

```
>>> letters.extend(['b', 'a'])
```

```
['a', 'b', 'd', ['e'], 'b', 'a']
```

```
>>> letters.insert(2, 'c')
```

```
['a', 'b', 'c', 'd', ['e'], 'b', 'a']
```

```
>>> letters.remove('a')
```

```
['b', 'c', 'd', ['e'], 'b', 'a']
```

```
>>> letters.reverse()
```

```
['a', 'b', ['e'], 'd', 'c', 'b']
```

```
>>> letters.pop()
```

```
'b'
```

```
>>> letters
```

```
['a', 'b', ['e'], 'd', 'c']
```


List Indexing

```
>>> letters = ['a', 'b', 'c', 'd', 'e']
```

```
>>> letters[:]
```

```
['a', 'b', 'c', 'd', 'e']
```

```
>>> letters[2:]
```

```
['c', 'd', 'e']
```

```
>>> letters[:2]
```

```
['a', 'b']
```

```
>>> letters[:-2]
```

```
['a', 'b', 'c']
```

```
>>> letters[::-2]
```

```
['a', 'c', 'e']
```

```
>>> letters[::-1]
```

```
['e', 'd', 'c', 'b', 'a']
```

```
>>> letters[1:4:2]
```

```
['b', 'd']
```

List Comprehensions

A fast, pythonic trick!

Create a **new** list using the values in an existing one:

```
L1 = [0, 4, 8, 16]
```

```
L2 = [x ** 2 for x in L1]
```

```
print(L1)
```

```
print(L2)
```

```
>>> [0, 4, 8, 16]
```

```
>>> [0, 16, 64, 256]
```

Tuples

Like lists, but immutable

```
t1 = (1, 2, 3, "abc")
```

```
t2 = ( 5, 6, t1)
```

Operations:

Concatenation: `t1 + t2` `(1, 2, 3, 'abc', 5, 6, (1, 2, 3, 'abc'))`

Indexing: `(t1+t2) [3]` `'abc'`

Slicing: `(t1+t2) [1:3]` `(2, 3)`

- You can iterate over tuples
- You cannot mutate tuples
- Can be used as keys in the dictionary (lists can't) - **why?**

Dictionaries

- Key, value pairs
- Keys can be integers, strings, tuples, etc. (anything **immutable**)
- Keys can't be lists, dictionaries, etc. (anything mutable)
- Keys are unique, values don't have to be

True

T/F Question: In Python, the keys of a dict must be immutable.

T/F Question: The dictionary {'a': '1', 'b': '2', 'c': '3'} has a mapping of string: int

False

Using Dictionaries

```
>>> zoo = {'elephant' : 3, 'giraffe' : 4}
>>> len(zoo)
2
>>> zoo['elephant']
3
>>> zoo['frog']
KeyError: 'frog'
>>> zoo.get('frog', 'Frog is not in zoo')
'Frog is not in zoo'
>>> if 'cheetah' not in zoo:
    zoo['cheetah'] = 5
```

```
>>> zoo
{'cheetah': 5, 'giraffe': 4, 'elephant': 3}
>>> list(zoo.keys())
['cheetah', 'giraffe', 'elephant']
>>> list(zoo.values())
[5, 4, 3]
>>> del zoo['elephant']
>>> zoo
{'cheetah': 5, 'giraffe': 4}
```

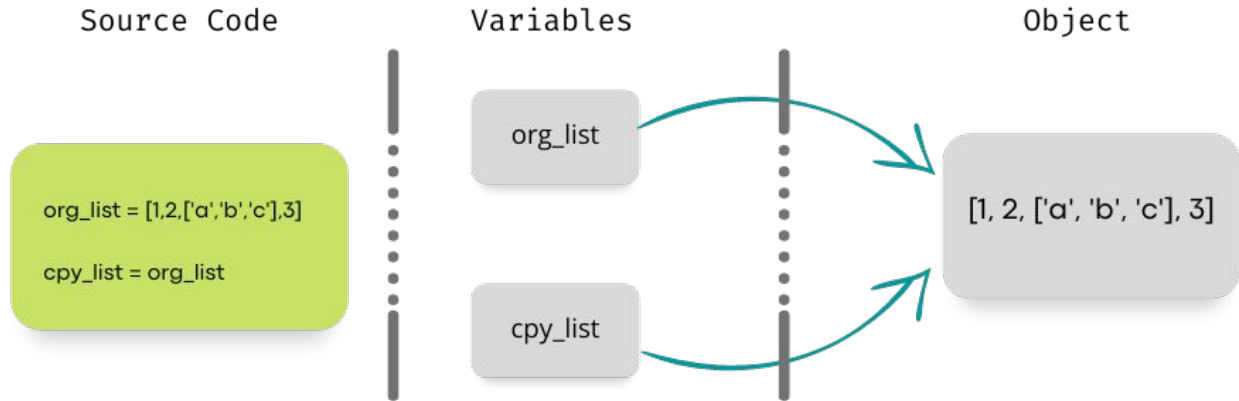
Mutability & Aliasing

Mutable: Lists, Dictionaries, Sets

Immutable: Strings, int, float, bool, tuples

Aliasing: Two variables bound to the same object

```
>>> a = [1]
>>> b = a
>>> a.append(2)
>>> print(a)
[1, 2]
>>> print(b)
[1, 2]
```



Mutability: Lists

```
L1 = ['a', 'b', 'c']  
L2 = [ [], L1, 1]  
L3 = [ [], ['a', 'b', 'c'], 1]  
L4 = [L1]+L1  
L2[1][2]='z'  
print( 'L1 = ', L1 )  
print( 'L2 = ', L2 )  
print( 'L3 = ', L3 )  
print( 'L4 = ', L4 )
```

What is going to be printed?

```
L1 = ['a', 'b', 'z']  
L2 = [ [], ['a', 'b', 'z'], 1]  
L3 = [ [], ['a', 'b', 'c'], 1]  
L4 = [['a', 'b', 'z'], 'a', 'b', 'c']
```

Cloning

```
L1 = ['a', 'b', 'c']
```

```
L2 = L1[:]
```

```
print( 'L1 = ', L1 )
```

```
print( 'L2 = ', L2 )
```

```
L1.append('d')
```

```
print( 'L1 = ', L1 )
```

```
print( 'L2 = ', L2 )
```

What is going to be printed?

```
L1 = ['a', 'b', 'c']
```

```
L2 = ['a', 'b', 'c']
```

```
L1 = ['a', 'b', 'c', 'd']
```

```
L2 = ['a', 'b', 'c']
```




Questions?



Abstraction & Decomposition

How to think about and solve complex systems at a high-level:

- **break up** a problem into simpler building blocks
- give each block a **name**, forget about the details of how it's built, just know its **inputs** and **outputs**

Abstraction & Decomposition

Why abstract and decompose?

- better code organization
- fewer lines of code
- can test small units (testing full system may be unmanageable)

Abstraction & Decomposition

How do we abstract and decompose?

Functions !!!

the most basic unit of code abstraction

Variables abstract values

Functions abstract blocks of code

Functions

1. name

2. Inputs
(parameters)

3. Promises a certain behavior
(if given proper inputs)

```
def function_name(arg1, arg2, ..., argN):  
    '''  
    docstring here (can specify the function's promise)  
    '''  
    #some code  
    #some more code  
    return something
```

Functions

Calling a function $\Rightarrow$ running it, with specific parameters

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Calling a function $\Rightarrow$ running it, with specific parameters

How to call a function:

- specify name
- *pass* the parameters
- optionally, save the returned output

```
out = function_name(x1, x2, ..., xn)
```

Functions examples

function definition

```
def even_or_odd(number):  
    '''  
    Returns True if number is even, False otherwise  
    '''  
    if number % 2 == 0 :  
        return True  
    else:  
        return False
```

function call

```
three_is_even = even_or_odd(3)
```

Question: what's the difference between **even_or_odd()** and **even_or_odd** in code?

Functions examples

```
def mult_by_five(number):  
    print(number * 5)
```

```
mult_by_five("hi")
```

what does this do?

Prints: hihihihhi

what is returned by `mult_by_five` ? None!

Lambda functions

A way to define a short function in one line, often to be used as an argument to another function:

```
def run_function_twice(a_function, param1, param2):  
    """  
    a_function: A function with one parameter  
    param1: The input to the function to run the first time  
    param2: The input to the function to run the second time  
    """  
    print(a_function(param1))  
    print(a_function(param2))  
  
func = lambda x: x ** 2 + 2 * x + 1  
  
run_function_twice(func, 2, 3) # prints 9, 16
```



Questions?



Scope

scope dictates what parts of a program can see each variable's value

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- a scope is a table, mapping variable names to values
 - assignment (`<variable> = <expression>`) adds an item to the table

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Scope

scope dictates what parts of a program can see each variable's value

- a scope is a table, mapping variable names to values
 - assignment (<variable> = <expression>) adds an item to the table
- when your program starts, there's one scope called *global* scope
- when you call a function, a new scope is created
 - the scope is destroyed when the function returns

Scope

How is scope used?

- when a variable is used in an expression, the variable is looked up in the current scope

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Scope

How is scope used?

- when a variable is used in an expression, the variable is looked up in the current scope
 - if not found, the variable is looked up in the scope where the function was defined
 - if not found there, repeat until found or we hit global scope and still not found

Scope

global

x = 5

y = 8

```
def my_function(x):
```

```
    y = 10
```

```
    print(y) 10
```

```
    return x * y
```

```
print(my_function(9)) 90
```

```
print(x) 5
```

```
print(y) 8
```

Exam Question

```
def testprog(x, y):  
    temp = x  
    x = y  
    y = temp  
    print(x)
```

```
x = 3  
y = -3  
print(x) 3  
testprog(x, y) -3  
print(x) 3
```

What is going to be printed?

Scope

```
def f(x):  
    print('In f(x): x =', x)  
    print('In f(x): y =', y)  
    def g():  
        print('In g(): x =', x)  
    g()
```

```
x = 3  
y = 2  
f(1)
```

in f(x): x = 1

in f(x): y = 2

in g(): x = 1



Questions?



Recursion

a *recursive* function is any function that calls itself

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Two crucial structural characteristics:

- *Base case*: a simplest version of the input
 - no recursive calls in base case

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Two crucial structural characteristics:

- *Base case*: a simplest version of the input
 - no recursive calls in base case
- *Recursive case*: makes one or more recursive calls with a simpler input
 - recursive calls **must** bring us closer to the base case
 - some basic computation is done in addition to the recursive calls

Recursion

When to use recursion?

Recursion

When to use recursion?

when a problem can be solved easily *if*
we have the answer to a subproblem of the same form

Recursion examples

Integer multiplication

$$a * b = a + a * (b - 1)$$

Factorial

$$n! = n * (n - 1)!$$

Fibonacci

$$\text{fib}(n) = \text{fib}(n - 1) + \text{fib}(n - 2)$$

Recursion examples

Integer multiplication

$$a * b = a + a * (b - 1)$$

```
def recurMul(a, b):  
    if b == 1:  
        return a  
    else:  
        return a + recurMul(a, b-1)
```

Recursion examples

Factorial

$$n! = n * (n-1)!$$

```
def factR(n):  
    """assumes that n is  
    an int > 0  
    returns n!"""  
    if n == 1:  
        return n  
    return n*factR(n-1)
```

Recursion examples

Fibonacci

fib(n) = fib(n-1) + fib(n-2)

```
def fib(x):  
    """assumes x an int >= 0  
        returns Fibonacci of x"""  
    assert type(x) == int and x >= 0  
    if x == 0 or x == 1:  
        return 1  
    else:  
        return fib(x-1) + fib(x-2)
```



Final Review Session Part 2



Complexity

- An algorithm might be useless if it takes too long to get an answer
- We need a notion to measure how long an algorithm takes
- We would like our notion to be independent of the machine it runs on

Big O? Θ ? Ω ?

$O(g(n))$

Describes an **upper bound** on the runtime complexity

$\Omega(g(n))$

Describes a **lower bound** on the runtime complexity

$\Theta(g(n))$

Describes the **tight (upper and lower) bound** on the runtime complexity

Big Θ Notation

- Describes the runtime of an algorithm as a function of its input size
- Typically describes the worst case runtime
 - “In the worst case, how much time will it take for this algorithm to run?”
- When describing an algorithm, choose the tightest bound

Examples

I have a function $f(x) = 3x^2 + 2x + 1$

$O(g(n))$

Can be $O(n^2)$, because there exists $g(n) = 4x^2$ that will surpass $f(x)$

But could also be $O(n^3)$, for example, since it will always surpass $f(x)$

$\Omega(g(n))$

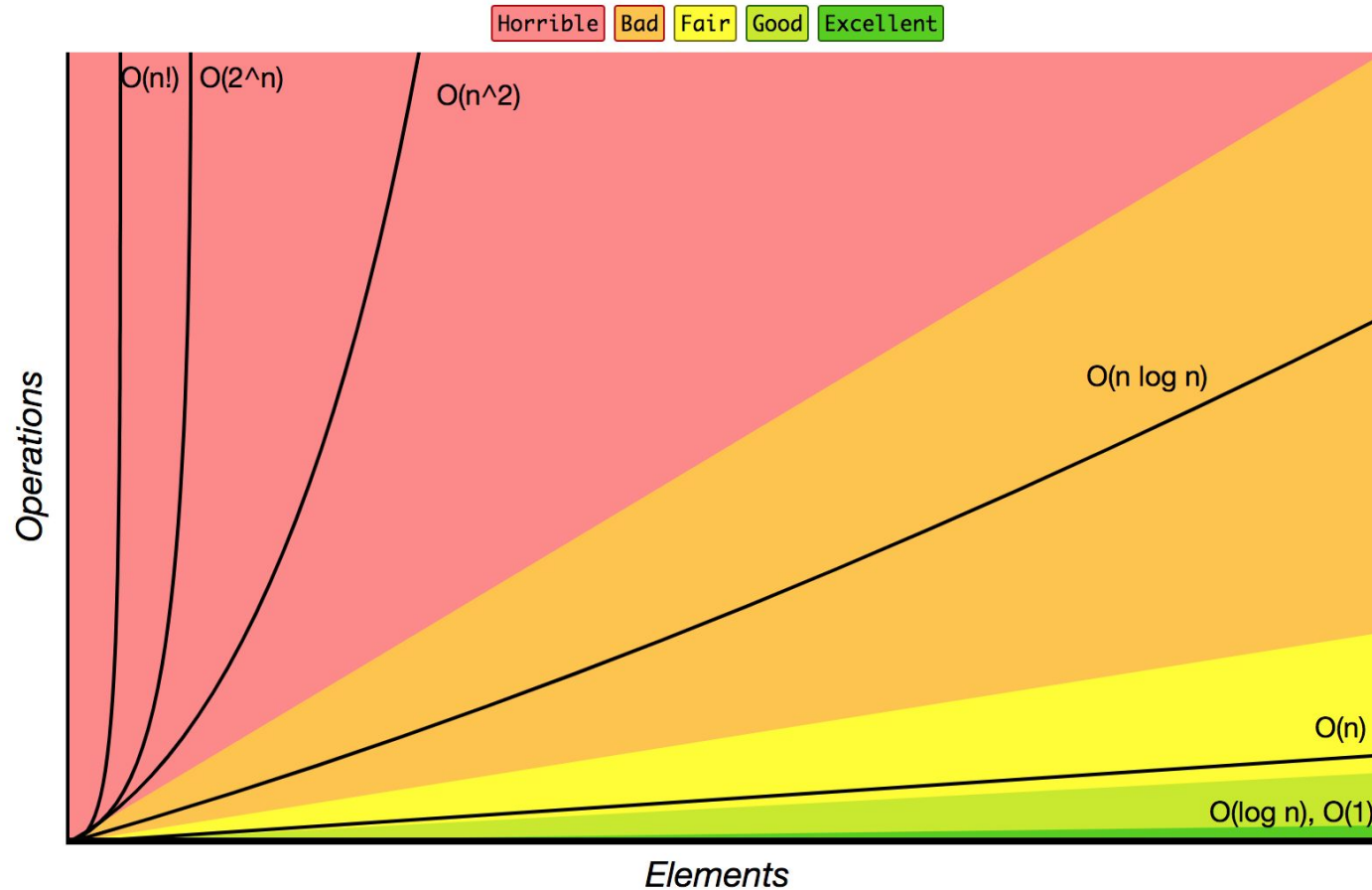
Could be $\Omega(n)$, meaning the complexity will always surpass $g(n) = n$

$\Theta(g(n))$

Must be $\Theta(n^2)$, because it is both an upper and lower bound

i.e. $4x^2$ and x^2

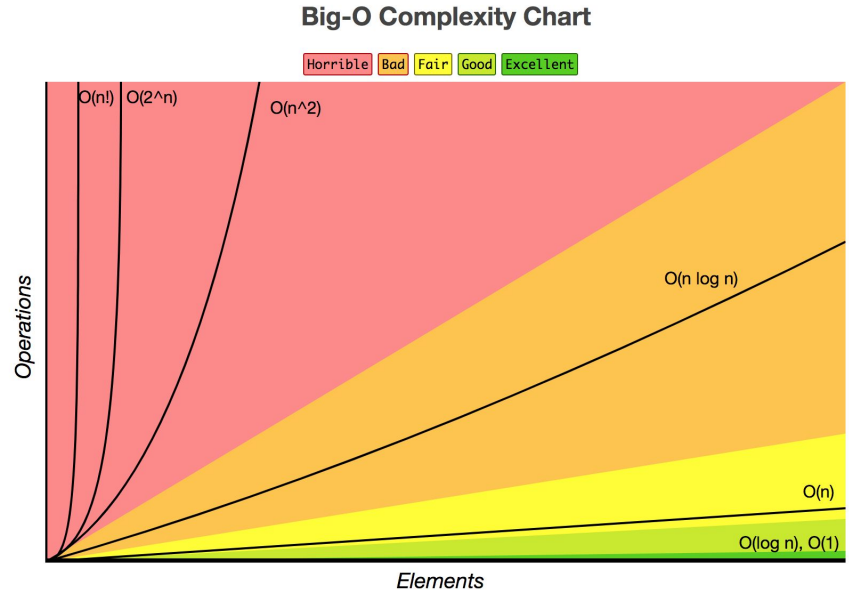
Big-O Complexity Chart



Big Θ Notation Mechanics

Fastest growing term dominates:

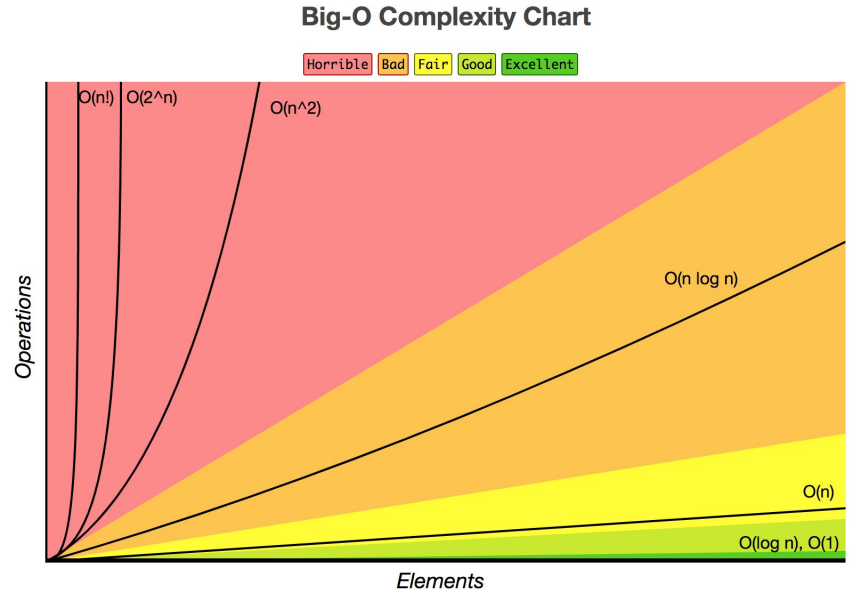
$$n^2 + 100n + 1000 \log(n)$$



Big Θ Notation Mechanics

Fastest growing term dominates:

$$n^2 + 100n + 1000 \log(n) = \Theta(n^2)$$



Big Θ Notation Mechanics

Fastest growing term dominates:

$$n^2 + 100n + 1000 \log(n) = \Theta(n^2)$$

Constant factors do not affect complexity:

$$10000000000n$$

$$0.00000001n$$

Big Θ Notation Mechanics

Fastest growing term dominates:

$$n^2 + 100n + 1000 \log(n) = \Theta(n^2)$$

Constant factors do not affect complexity:

<- WHY??

$$\cancel{10000000000}n = \Theta(n) = \cancel{0.00000001}n$$

Commonly Used Complexities in Algorithms

$\Theta(1)$ - Constant

$\Theta(\log n)$ - Logarithmic

$\Theta(n)$ - Linear

$\Theta(n \log n)$ - Log-Linear

$\Theta(n^k)$ - Polynomial

$\Theta(k^n)$ - Exponential

Complexity of built-in methods

- **Constant-time, $\Theta(1)$**

- Assignment, $x=2$
- Basic operations, $+ - * / > <$

- **Dictionary**

- Look-up: $\Theta(1)$
- Length: $\Theta(1)$
- Insert: $\Theta(1)$
- Delete: $\Theta(1)$
- `dictionary.keys()`: $\Theta(n)$ - because a list is generated
- Check if a key is in the dictionary: $\Theta(1)$

Complexity of built-in methods

- **List**

- Append: $\Theta(1)$
- Length: $\Theta(1)$
- Insert: $\Theta(n)$
- Delete: $\Theta(n)$
- Copy: $\Theta(n)$
- Sort: $\Theta(n \log n)$
- Check if an item is in the list: $\Theta(n)$
 - “if elt in a_list:”

Strategies for analyzing complexity

- Loops
 - # of iterations in the loop
 - Amount of work within each loop
- Recursive calls
 - # of recursive calls that are made
 - Amount of work done for each recursive call

Total Time = Time per Iteration * # of Iterations
or Time per Call * # of Calls

What is the complexity?

```
def beep(n):
```

```
    tot = 0
```

```
    while n >= 2:
```

Complexity: $\Theta(\log n)$

```
        tot += n
```

```
        n = n // 2
```

```
    return tot
```

What is the complexity?

```
def is_palindrome_iterate(s):  
    `` input size, n = len(s) ``  
    string_len = len(s)  
    i = 0  
    while i < string_len//2 +1:  
        if s[i] != s[-i-1]:  
            return False  
        i+=1  
    return True
```

Number of iterations: $\Theta(n)$

Number of operations in each iteration: constant

Complexity: $\Theta(n)$

What is the complexity?

```
def is_palindrome_recursive(s):  
    if len(s) == 0: return True  
  
    if len(s) == 1: return True  
  
    else:  
        first_char = s[0]  
        last_char = s[-1]  
        if first_char == last_char:  
            return is_palindrome_recursive(s[1:-1])  
        else:  
            return False
```

$n/2$ recursive calls: $\Theta(n)$
Slicing strings: $\Theta(n)$
Complexity: $\Theta(n^2)$

 Slicing a string = $O(n)$



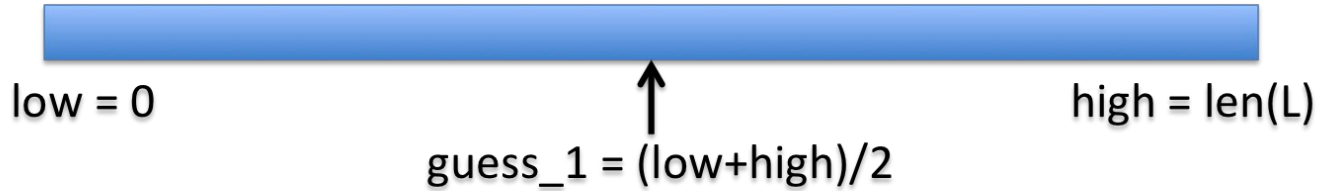
Questions?



Search

- Linear search
 - Brute force search
 - List doesn't have to be sorted
 - $\Theta(n)$
- Bisection search
 - List must be sorted to give correct answer
 - $\Theta(\log n)$

Bisection search



Complexity of searching unsorted list

- Linear search
 - $\Theta(n)$
 - One time search
- Bisection search
 - $\text{complexity}(\text{sort}) + \text{complexity}(\text{bisection search})$
 - $\text{complexity}(\text{sort}) + \Theta(\log n)$
 - $\text{complexity}(\text{sort}) > \Theta(n)$, always

Sorting Methods: Bubble Sort

- Each step, for $i = 0, 1, \dots, \text{len}(L)-2$, swap $L[i], L[i+1]$ such that smaller is first
- Checks every adjacent pair in list to see if it is sorted
- n steps to put everything in order, building right to left
- Up to n passes



First Pass

(**5** 1 4 2 8) $\rightarrow$ (**1** **5** 4 2 8)
(1 **5** **4** 2 8) $\rightarrow$ (1 **4** **5** 2 8)
(1 4 **5** 2 8) $\rightarrow$ (1 4 **2** 5 8)
(1 4 2 **5** 8) $\rightarrow$ (1 4 2 **5** 8)

Second Pass

(**1** **4** 2 5 8) $\rightarrow$ (**1** **4** 2 5 8)
(1 **4** **2** 5 8) $\rightarrow$ (1 **2** **4** 5 8)
(1 2 **4** 5 8) $\rightarrow$ (1 2 **4** 5 8)
(1 2 4 **5** 8) $\rightarrow$ (1 2 4 **5** 8)

Third Pass

(**1** **2** 4 5 8) $\rightarrow$ (**1** **2** 4 5 8)
(1 **2** **4** 5 8) $\rightarrow$ (1 **2** **4** 5 8)
(1 2 **4** 5 8) $\rightarrow$ (1 2 **4** 5 8)
(1 2 4 **5** 8) $\rightarrow$ (1 2 4 **5** 8)

Sorting Methods: Bubble Sort

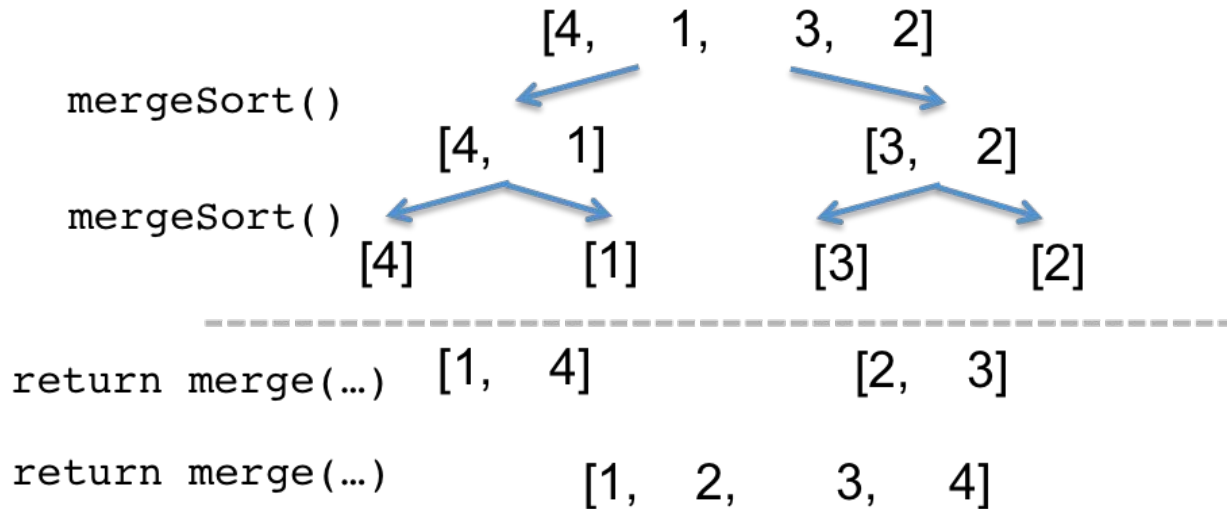
- How many steps?
- Each step, how many operations?
- Complexity?

Sorting Methods: Bubble Sort

- How many steps? $\Theta(n)$
- Each step, how many operations? $\Theta(n)$
- Complexity? $\Theta(n^2)$

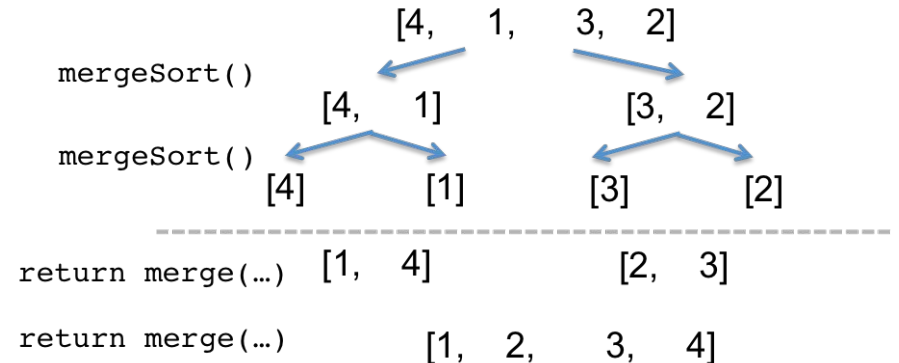
Sorting Methods: Merge Sort

- Break list in half
- Recursively sort both halves
- Merge the sorted halves



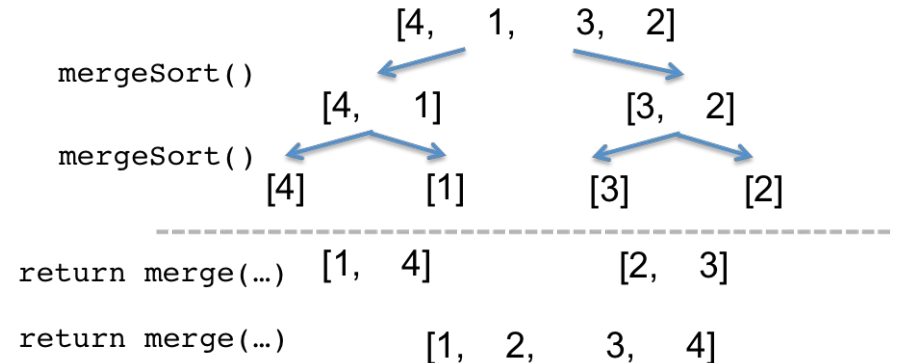
Sorting Methods: Merge Sort

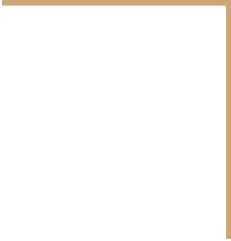
- How many levels of the recursive tree?
- How much computation of each level of the tree?
- Complexity?



Sorting Methods: Merge Sort

- How many levels of the recursive tree? $O(\log n)$
- How much computation of each level of the tree? $O(n)$
- Complexity? $O(n \log n)$





Questions?



Debugging

- Assertions

```
assert <boolean condition>
```

```
assert <boolean condition>, <argument>
```

- Exception

```
try:
```

```
    <code>
```

```
except <exception_type>:
```

```
    <other code to run if try block encounters an exception>
```

```
finally:
```

```
    <always executed after try, else, and except clauses>
```

Assertion Error

```
x = 3
```

```
assert x == 4, 'x is not 4'
```

throws an AssertionError, stops all further computation

Exception Types

- **NameError**: access a name to a variable
 - ex. `NameError: name 'variable_name' is not defined`
- **ValueError**: concatenating a non-string with a string
- **IndexError**: accessing beyond the limits of a list
 - ex. `IndexError: list index out of range`
- **KeyError**: attempting to use a key in a dict that doesn't exist
 - ex. `KeyError: 'key_name'`
- **TypeError**: converting an inappropriate type
 - ex. `TypeError: unsupported operand type(s) for +: 'int' and 'str'`
- **AttributeError**: trying to append to a string
 - ex. `AttributeError: 'str' object has no attribute 'append'`

Input Space Partitioning

```
def search_odd(a, b):  
    """  
    Inputs  
        a, b: integers or booleans  
    Outputs  
        True if either input is equal to True or odd, and False otherwise  
    """  
    if type(a) == bool:  
        if a:  
            return True  
    else:  
        if a%2 == 1:  
            return True  
    if type(b) == bool:  
        if b:  
            return True  
    else:  
        if b%2 == 1:  
            return True  
    return False
```

Characterizing all types of input a program might allow based on its specification

Input Space Partitioning

```
def search_odd(a, b):  
    """  
    Inputs  
        a, b: integers or booleans  
    Outputs  
        True if either input is equal to True or odd, and False otherwise  
    """  
    if type(a) == bool:  
        if a:  
            return True  
    else:  
        if a%2 == 1:  
            return True  
    if type(b) == bool:  
        if b:  
            return True  
    else:  
        if b%2 == 1:  
            return True  
    return False
```

Inputs: {bools}, {ints}

Can subdivide each of those sets:

{bools} $\rightarrow$ {True}, {False}

{ints} $\rightarrow$ {evens}, {odds}

Classes

- Classes provide a means of bundling data and functionality together
- They have **attributes** and **methods** specific to themselves

```
class Vehicle(object):  
    def __init__(self, name):  
        self.name = name # a variable  
    def honk(self): # a method  
        print(self.name, "says HONK")
```

Classes

- You can use classes to instantiate **objects**

```
>>> my_vehicle = Vehicle("batmobile")
>>> print(my_vehicle.name)
batmobile
>>> my_vehicle.honk()
batmobile says HONK
```

```
class Vehicle:
    def __init__(self, name):
        self.name = name # a variable
    def honk(self): # a method
        print(self.name, "says HONK")
```

Classes

- Calling class methods

```
>>> my_vehicle = Vehicle("batmobile")
>>> print(my_vehicle.name)
batmobile
>>> my_vehicle.honk()
batmobile says HONK
>>> my_vehicle.honk
<bound method Vehicle.honk of <__main__.Vehicle instance at
0x1010748c0>>
```

```
class Vehicle:
    def __init__(self, name):
        self.name = name # a variable
    def honk(self): # a method
        print(self.name, "says HONK")
```

Classes

- Calling class methods

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>>> my_vehicle = Vehicle("batmobile")
```

```
>>> print(my_vehicle.name)
```

```
batmobile
```

```
>>> my_vehicle.honk()
```

```
batmobile says HONK
```

```
>>> my_vehicle.honk
```

```
<bound method Vehicle.honk of <__main__.Vehicle instance at  
0x1010748c0>>
```

What does this mean?

Classes

```
class Vehicle:
    def __init__(self, name):
        self.name = name # a variable
    def honk(self): # a method
        print(self.name, "says HONK")
```

- Calling class methods

```
>>> my_vehicle = Vehicle("batmobile")
```

```
>>> print(my_vehicle.name)
```

```
batmobile
```

```
>>> my_vehicle.honk()
```

```
batmobile says HONK
```

```
>>> my_vehicle.honk
```

```
<bound method Vehicle.honk of <__main__.Vehicle instance at  
0x1010748c0>>
```

```
>>> Vehicle.honk
```

```
<unbound method Vehicle.honk>
```

Classes

```
class Vehicle:
    def __init__(self, name):
        self.name = name # a variable
    def honk(self): # a method
        print(self.name, "says HONK")
```

- Calling class methods

```
>>> my_vehicle = Vehicle("batmobile")
```

```
>>> print(my_vehicle.name)
```

```
batmobile
```

```
>>> my_vehicle.honk()
```

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batmobile says HONK
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```
>>> my_vehicle.honk
```

```
<bound method Vehicle.honk of <__main__.Vehicle instance at  
0x1010748c0>>
```

```
>>> Vehicle.honk
```

```
<unbound method Vehicle.honk>
```

what??

Classes

- Calling class methods

```
>>> my_vehicle = Vehicle("batmobile")
>>> print(my_vehicle.name)
batmobile
>>> my_vehicle.honk()
batmobile says HONK
>>> my_vehicle.honk
<bound method Vehicle.honk of <__main__.Vehicle instance at 0x1010748c0>>
>>> Vehicle.honk
<unbound method Vehicle.honk>
>>> Vehicle.honk()
Traceback (most recent call last):
  File "<stdin>", line 1, in <module>
TypeError: unbound method honk() must be called with Vehicle instance as
first argument (got nothing instead)
>>> Vehicle.honk(my_vehicle)
batmobile says HONK
```

Classes

```
class Vehicle:  
    def __init__(self, name):  
        self.name = name # a variable  
    def honk(self): # a method  
        print(self.name, "says HONK")
```

- Calling class methods

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>>> my_vehicle = Vehicle("batmobile")  
>>> print(my_vehicle.name)  
batmobile  
>>> my_vehicle.honk()  
batmobile says HONK  
>>> my_vehicle.honk  
<bound method Vehicle.honk of <__main__.Vehicle instance at 0x1010748c0>>  
>>> Vehicle.honk  
<unbound method Vehicle.honk>  
>>> Vehicle.honk()
```

WHAT

```
Traceback (most recent call last):  
  File "<stdin>", line 1, in <module>  
TypeError: unbound method honk() must be called with Vehicle instance as  
first argument (got nothing instead)  
>>> Vehicle.honk(my_vehicle)  
batmobile says HONK
```


Classes

```
class Vehicle:
    def __init__(self, name):
        self.name = name # a variable
    def honk(self): # a method
        print(self.name, "says HONK")
```

- You can use classes to instantiate objects

```
>>> my_vehicle = Vehicle("batmobile")
>>> print(my_vehicle.name)
batmobile
>>> my_vehicle.honk()
batmobile says HONK
>>> my_vehicle.honk -> Bound method: part of a specific object
<bound method Vehicle.honk of <__main__.Vehicle instance at 0x1010748c0>>
>>> Vehicle.honk
<unbound method Vehicle.honk> -> Unbound method: not part of an object
>>> Vehicle.honk()
Traceback (most recent call last):
  File "<stdin>", line 1, in <module>
TypeError: unbound method honk() must be called with Vehicle instance as
first argument (got nothing instead) -> we get an error because
>>> Vehicle.honk(my_vehicle)
batmobile says HONK
```

there is no data for the method to operate on